

14.69 ●●● A 1.70 kg, horizontal, uniform tray is attached to a vertical ideal spring of force constant 185 N/m and a 290 g metal ball is in the tray. The spring is below the tray, so it can oscillate up and down. The tray is then pushed down to point *A*, which is 16.1 cm below the equilibrium point, and released from rest. (a) How high above point *A* will the tray be when the metal ball leaves the tray? (*Hint*: This does *not* occur when the ball and tray reach their maximum speeds.) (b) How much time elapses between releasing the system at point *A* and the ball leaving the tray? (c) How fast is the ball moving just as it leaves the tray?

146g.

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Dienblad: $m = 1,70 \text{ kg}$ $k = 185 \text{ N/m}$

$M_{\text{bal}} = 290 \text{ g} = 0,290 \text{ kg}$ naar beneden tot A.
naar beneden het blad.

$A = 16,1 \text{ cm} = 0,161 \text{ m}$

$$F_{z_1} = F_{z \text{ blad}} + F_{z \text{ bal.}}$$

Indrukken blad
los lab.

Wanneer komt
 $m = 0,290 \text{ kg}$
hither los?

Boek: $F_{\text{d veer}} = k \cdot d$ $x = A \text{ en } t = 0 \rightarrow \varphi = 0$

hoger los: $\frac{k \cdot d}{m} = g$ (m : totale massa)

$$d = \frac{m \cdot g}{k} = \frac{(1,7 + 0,29) \cdot 9,81}{185} = 10,54 \text{ cm}$$

14.6g ver.

Dit is voorbij het evenwichtspunt

Boven A: $10,54 + 16,1 = 26,6 \text{ cm}$

Moraal: $d = \frac{m \cdot g}{m}$: m totaal nemen

dit is meer negatief dan g
→ a = g
F_{even} = k · d.
 $\frac{a}{m} = k \cdot d.$

xx b.

Gev. t, wanneer de bal loslaat : A = 26,6 cm

$x = A \cdot \cos(\omega \cdot t) \rightarrow \omega = \sqrt{\frac{k}{m}} = \sqrt{\frac{105}{1,99}} = \sqrt{52,96} = 9,64 \text{ rad/sec}$

$10,54 = 16,1 \cdot \cos(9,64 \cdot t)$

$\cos 9,64 t = \frac{-10,54}{16,1} = -0,6547 \rightarrow 9,64 t = \overset{2,28458}{0,8571}$

→ $t = \frac{2,28458}{9,64} = 0,237 \text{ sec.}$

c

v_t
Op t

$v_t = -A \omega \cdot \sin(\omega \cdot t)$

$= -0,161 \cdot 9,64 \cdot \sin(9,64 \cdot 0,237)$

$= +1,52 \cdot \sin(2,28)$

$= +1,52 \cdot 0,7558 \dots = 1,17 \text{ m/s}$

Boek: $v = \sqrt{\frac{k}{m}(A^2 - x^2)} = \sqrt{\frac{105}{1,99} \cdot (0,161)^2 - (-0,1054)^2}$

a: Dozent: $x(t) = 16,1 \cos(\omega \cdot t)$
 $v(t) = 16,1 \omega \sin(\omega \cdot t)$
 $a(t) = -16,1 \omega^2 \cos \omega \cdot t$

→ meter en kogel komt los: $-9,81 = 0,161 \cdot 9,64^2 \cos \omega t$

$\cos \omega t = \frac{-9,81}{0,161 \cdot 9,64^2} = -0,65$

$\omega t = \cos^{-1}(-0,65) = 2,28 \text{ rad}$

naarom $x(t) = -16,1 \cdot -0,65 = 10,56 \text{ cm}$

$h = 16,1 + 10,5 = 26,6 \text{ cm.}$

b) $\omega t = 2,28 \rightarrow t = \frac{2,28}{9,64} = 0,245$

c) $v(t) = 16,1 \cdot 9,64 \cdot \sin(2,28) = 117 \text{ cm/sec}$
 $= 1,17 \text{ m/s.}$

positief klopt: beweging is omhoog